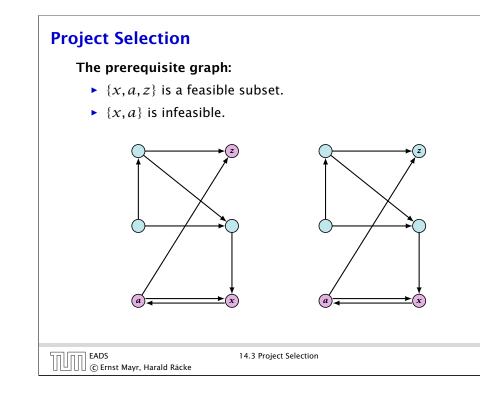
### **Baseball Elimination**

Proof (⇒)

- Suppose we have a flow that saturates all source edges.
- We can assume that this flow is integral.
- For every pairing x-y it defines how many games team x and team y should win.
- The flow leaving the team-node x can be interpreted as the additional number of wins that team x will obtain.
- This is less than  $M w_x$  because of capacity constraints.
- Hence, we found a set of results for the remaining games, such that no team obtains more than M wins in total.
- Hence, team *z* is not eliminated.

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# **Project Selection**

**Project selection problem:** 

- Set *P* of possible projects. Project *v* has an associated profit *p<sub>v</sub>* (can be positive or negative).
- Some projects have requirements (taking course EA2 requires course EA1).
- Dependencies are modelled in a graph. Edge (u, v) means "can't do project u without also doing project v."
- ► A subset *A* of projects is feasible if the prerequisites of every project in *A* also belong to *A*.

Goal: Find a feasible set of projects that maximizes the profit.

EADS 14.3 Project Selection

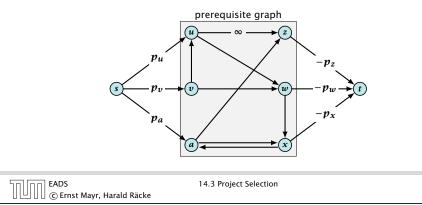
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## **Project Selection**

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#### Mincut formulation:

- Edges in the prerequisite graph get infinite capacity.
- ► Add edge (s, v) with capacity p<sub>v</sub> for nodes v with positive profit.
- ► Create edge (v, t) with capacity -pv for nodes v with negative profit.



### Theorem 84

A is a mincut if  $A \setminus \{s\}$  is the optimal set of projects.

#### Proof.

