## Baseball Elimination

## Proof ( $\Rightarrow$ )

- Suppose we have a flow that saturates all source edges.
- We can assume that this flow is integral.
- For every pairing $x-y$ it defines how many games team $x$ and team $y$ should win.
- The flow leaving the team-node $x$ can be interpreted as the additional number of wins that team $x$ will obtain.
- This is less than $M-w_{x}$ because of capacity constraints.
- Hence, we found a set of results for the remaining games, such that no team obtains more than $M$ wins in total.
- Hence, team $z$ is not eliminated.


## Project Selection

## The prerequisite graph:

- $\{x, a, z\}$ is a feasible subset.
- $\{x, a\}$ is infeasible.



## Project Selection

## Project selection problem:

- Set $P$ of possible projects. Project $v$ has an associated profit $p_{v}$ (can be positive or negative).
- Some projects have requirements (taking course EA2 requires course EA1).
- Dependencies are modelled in a graph. Edge $(u, v)$ means "can't do project $u$ without also doing project $v$."
- A subset $A$ of projects is feasible if the prerequisites of every project in $A$ also belong to $A$.

Goal: Find a feasible set of projects that maximizes the profit.
13.3 Project Selection

## Project Selection

## Mincut formulation:

- Edges in the prerequisite graph get infinite capacity.
- Add edge $(s, v)$ with capacity $p_{v}$ for nodes $v$ with positive profit.
- Create edge $(v, t)$ with capacity $-p_{v}$ for nodes $v$ with negative profit.


Theorem 2
$A$ is a mincut if $A \backslash\{s\}$ is the optimal set of projects.

## Proof.

- $A$ is feasible because of capacity infinity edges.
- $\operatorname{cap}(A, V \backslash A)=$ $\qquad$ ' the capacity of the cut - $(A, V \backslash A)$ corresponds to maximizing profits of projects in $A$
$p_{v}+$ $\qquad$ $\left(-p_{v}\right)$
$\square$


