# **Project Selection**

### Project selection problem:

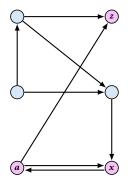
- Set P of possible projects. Project v has an associated profit  $p_v$  (can be positive or negative).
- Some projects have requirements (taking course EA2 requires course EA1).
- ▶ Dependencies are modelled in a graph. Edge (u, v) means "can't do project u without also doing project v."
- ▶ A subset *A* of projects is feasible if the prerequisites of every project in *A* also belong to *A*.

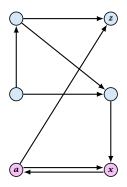
Goal: Find a feasible set of projects that maximizes the profit.

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## The prerequisite graph:

- $\{x, a, z\}$  is a feasible subset.
- $\{x, a\}$  is infeasible.

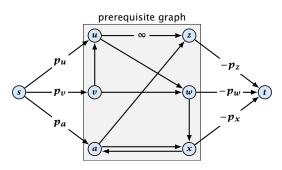




## **Project Selection**

#### Mincut formulation:

- Edges in the prerequisite graph get infinite capacity.
- Add edge (s, v) with capacity  $p_v$  for nodes v with positive profit.
- Create edge (v,t) with capacity  $-p_v$  for nodes v with negative profit.

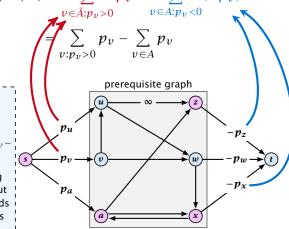


#### Theorem 2

A is a mincut if  $A \setminus \{s\}$  is the optimal set of projects.

#### Proof.

- A is feasible because of capacity infinity edges.



define  $p_s := 0$ . The step follows by adding  $\sum_{v \in A: p_v > 0} p_v - \sum_{v \in A: p_v > 0} p_v = 0$ . Note that minimizing

For the formula we

the capacity of the cut  $(A, V \setminus A)$  corresponds to maximizing profits of projects in A.